



Preferred Alignments of Angular Momentum Vectors of Galaxies in the SDSS Supercluster S[202-001+0084]

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Abstract

We present a study of spin vector orientation of 1331 SDSS (Sloan Digital Sky Survey) galaxies in SDSS Supercluster S[202-001+0084] having redshift 0.02 to 0.03. The data are provided by our collaborator, Institute of Astro-particle Physics, Innsbruck University, Austria. We have converted two dimensional data to three dimensional by Godlowskian Transformation. Our aim is to find out non-random effects in the preferred alignments of angular momentum vectors of galaxies. In general, no preferred alignments angular momentum vectors of galaxies are noticed, supporting Hierarchy model of galaxy formation. In almost all sub samples the 1st order Fourier coefficient suggests that the angular momentum vectors are randomly oriented but other statistical tests suggest anisotropic distribution probably due to the binning effect and gravitational shearing effect.

Key words: SDSS, 2D-FGRS, SV, Supercluster.

Introduction

Modern cosmology is based on two fundamental assumptions: First, the dominant interaction on cosmological scales is gravity, and second, the cosmological principle is a good approximation to the universe. The cosmological principle states that the universe, smoothed over large enough scales, is essentially homogeneous and isotropic. ‘Homogeneity’ has the intuitive meaning that at a given time the universe looks the same everywhere, and ‘isotropy’ refers to the fact that for any observer moving with the local matter the universe looks (locally) the same in all directions. Von Weizsacker and Gamow (1951 & 1952) made it clear that the observed rotation of the galaxies is important for cosmology: the fact that the galaxies rotate may be clue to the physical conditions under which these systems formed. In the instability picture, one imagines that large irregularity like galaxies grew under the influence of gravity from small imperfections in the early Universe (Gamow & Teller, 1939; Peebles 1965, 1967). In this picture one must abandon the idea that the angular momentum of the galaxies was given as the initial value, or developed in some sort of primeval turbulence (as was proposed by von Weizsacker, 1951 and Gamow, 1952, for otherwise the galaxies would have formed too soon (Peebles, 1967). On the other hand, huge low redshift galaxy surveys such as the 2-degree field galaxy redshift survey (2dFGRS, Colless *et al.* 2001) and the Sloan Digital Sky Survey (SDSS, York,

et al. 2000) have convinced most cosmologists that not only is isotropy but also homogeneity is in fact a reasonable assumption for the universe. The Universe is homogeneous and isotropic on scales larger than 100 Mpc, but on smaller scales we observe huge deviations from the mean density in the form of galaxies, galaxy clusters, and the cosmic web being made of sheets and filaments of galaxies. How do structures grow in the universe and how can we describe them? The most accepted view on the formation and evolution of large scale structure is that it was formed as a consequence of the growth of primordial fluctuations by gravitational instability. In the current favored model, smaller structures collapse first and are later incorporated in larger collapsing structures in a bottom-up scenario that provides a natural explanation for the formation of galaxies, clusters, filaments and Super clusters.

There are three predictions about the spatial orientation of spin vectors of galaxies. These are the '*pancake model*', the '*hierarchy model*,' and the '*primordial vorticity theory*.' The '*pancake model*' (Doroshkevich, 1973; Doroshkevich & Shandarin, 1978) predicts that the spin vectors (SVs hereafter) of galaxies tend to lie within the cluster plane. According to the '*hierarchy model*' (Peebles, 1969), the directions of the SVs should be distributed randomly. The '*Primordial Vorticity Theory*' (Ozernoy, 1971, 1978; Stein 1974) predicts that the spin vectors of galaxies are distributed primarily perpendicular to the cluster plane.

Godlowskian Transformation

The three dimensional orientation of the SV of a galaxy is characterized by two angles: the polar angle (θ) between the galactic SV and a reference plane (here equatorial plane), and the azimuthal angle (ϕ) between the projection of a galactic SV on to this reference plane and the X-axis within this plane. The detail derivations of the expressions of the angles θ and ϕ are given in Flin & Godłowski (1986). When using equatorial coordinate system as reference, then θ and ϕ can be obtained from measurable quantities as follows:

$$\sin\theta = -\cos i \sin\alpha \pm \sin i \sin p \cos\delta \quad (1)$$

$$\sin\phi = (\cos\theta)^{-1} [-\cos i \cos\delta \sin\alpha + \sin i (\mp \sin p \sin\delta \sin\alpha \mp \cos p \cos\alpha)] \quad (2)$$

Where, i is the inclination angle, the angle between the normal to the galaxy plane and the observer's line-of-sight, α - is right ascension, δ is declination and p is position angle. The inclination angle can be computed from the formula

$$\cos^2 i = \frac{(q^2 - q^{*2})}{(1 - q^{*2})} \quad (3)$$

This expression is valid for oblate spheroids (Holmberg, 1946). Here, q and q^* represent the measured axial ratio (b/a) and the intrinsic flatness of the galaxy, respectively. Hiedmann *et al.* (1971) showed that the values of q^* range from 0.083 for Sd spirals to 0.33 for ellipticals. For the galaxies with unknown morphology $q^*=0.20$ is assumed Holmberg (1946).

Method of Analysis

Here we describe the procedure for the removal the selection effects to obtain the isotropic distributions for both θ and ϕ as given by Aryal & Saurer (2000). Theoretically, the isotropic distribution curve for polar angle is cosine and that for a azimuthal angle is the average distribution curve, with the

restriction that the database is free from selection effect. Aryal & Saurer (2000) concluded that any selections imposed on the database may cause severe changes in the shapes of the expected isotropic distribution curves. In their method, a true spatial distribution of the galaxy rotation axis is assumed to be isotropic. Then, due to the projection effects, i can be distributed as $\sin i$, B can be distributed $\cos B$, the variables α and p can be distributed randomly, and the equations(1,2) can be used to calculate the corresponding values of polar (θ) and azimuthal (φ). We run simulations in order to define expected isotropic distribution curves for both the θ and φ distributions. The isotropic distribution curves are based on simulations including 10^7 virtual galaxies. At first we observed the distributions of α , δ , p and i for the galaxies in our samples and distributed by creating 10^7 virtual galaxies for respective parameters. We use these numbers to make input file and the expected distribution by running simulation in MATLAB 15.0.

Results & Discussion

Any deviation from expected isotropic distribution will be tested using four statistical parameters, namely chi-square probability ($P > \chi^2$), auto correlation coefficient ($C/C(\sigma)$), first order Fourier coefficient ($\Delta_{11}/\sigma(\Delta_{11})$) and first order Fourier probability ($P > \Delta_1$). For an isotropy, the limit of chi-square probability $P(>\chi^2)$ is <0.050 , auto correlation coefficient ($C/C(\sigma)$) is >1.0 , first order Fourier coefficient ($\Delta_{11}/\sigma(\Delta_{11})$) is >1.5 and Fourier probability $P(>\Delta_1)$ is <0.150 respectively. Any 'hump' (more solutions than the expected) or 'dip' (less solutions than the expected) in the histogram will be discussed as a local effect in the samples. The statistics for the polar and azimuthal angle distributions is given in Table 1. In the statistics of θ , a negative value of first order Fourier coefficient suggests that the spin vectors of galaxies tend to be oriented perpendicular with respect to the equatorial coordinate system. Similarly, a positive value of first order Fourier coefficient suggests that the spin vectors of galaxies tend to be oriented parallel with respect to the equatorial coordinate system. Whereas, in the statistics of φ , a positive ($\Delta_{11}/\sigma(\Delta_{11})$) with significant value suggests that the spin vector projections of galaxies tend to point radially with respect to the center of the equatorial coordinate system. Similarly, a significant negative value of ($\Delta_{11}/\sigma(\Delta_{11})$) implies that the spin vector projection of galaxies tend to orient tangentially with respect to the equatorial coordinate system.

Table 1: Statistics of the polar and azimuthal angle distributions of galaxies in the Super cluster S[202-001+0084]. The first column represents the statistics used, $P(>\chi^2)$ represents the chi-square probability (second row). Similarly, $C/C(\sigma)$ represents the auto-correlation coefficient (third row). The last two rows give the first order Fourier coefficient ($\Delta_{11}/\sigma(\Delta_{11})$) and first order Fourier probability $P(>\Delta_1)$.

Statistics	Polar angle(θ)	Azimuthal angle (φ)
$P(>\chi^2)$	0.000	0.000
$C/C(\sigma)$	11.9	132.5
$\Delta_{11}/\sigma(\Delta_{11})$	-0.03	-0.71
$P(>\Delta_1)$	0.000	0.000

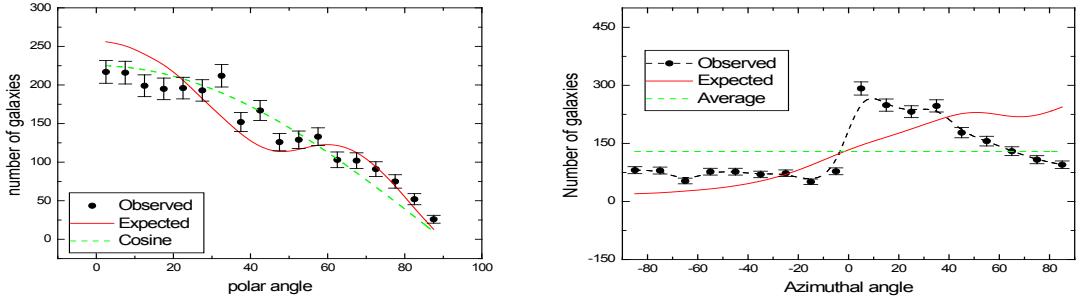


Figure 1: The polar (θ) and azimuthal (ϕ) angle distributions of galaxies in the SuperclusterS[202-001+0084]. The solid line represents the expected isotropic distributions. The dash lines represent the cosine and average distributions respectively. The solid circles with $\pm 1\sigma$ error bars are represent the observed distribution.

In addition to the statistical tests, we also study the 'humps' and 'dips' in the polar and azimuthal angle distributions. The solid curve, in the histogram of the θ -distribution, represents the expected isotropic distribution whereas, dashed curve is the cosine distribution. The solid circles with $\pm 1\sigma$ error bars represent the observed distribution. The shaded portion represents the range $0^\circ < \theta < 45^\circ$. A hump (or dip) in the smaller θ ($\theta < 45^\circ$) suggests that the spin vectors of galaxies tend to orient parallel (or perpendicular) with respect to the equatorial coordinate system. Similarly, a hump (or dip) in the larger θ ($\theta > 45^\circ$) suggests that the spin vectors of galaxies tend to orient perpendicular with respect to the equatorial coordinate system. In Figure 1, there is a hump on polar angle distribution at $\theta = 62^\circ$. This hump is due to 13 more observed solution than expected solutions in the range $\theta > 45^\circ$.

Similarly, a hump (or dip) in the larger ϕ indicates that the spin vectors of galaxies tend to be oriented perpendicular with respect to the equatorial coordinate system. In the histogram of the ϕ -distribution, solid curve represents the expected isotropic distribution whereas dashed curve is the average distribution. The solid circles with $\pm 1\sigma$ error bars represent the observed distribution. The shaded portion represents the range $-45^\circ < \phi < +45^\circ$. The humps and dips in the histograms of ϕ -distribution are not so easy to interpret as compared to θ -distributions. It is because the range of ϕ is -90° to $+90^\circ$. In the histogram of the ϕ -distribution, $\phi = 0^\circ$ means spin vector projections tend to point radially towards the center of the equatorial coordinate system. A hump in the middle (central eight bins) of the histogram suggests that the spin vector projections of galaxies tend to point towards the center of the chosen co-ordinate system. Similarly, a hump at first four and last four bins indicates that the spin vectors projections of galaxies tend to be oriented tangentially with respect to the chosen reference co-ordinate system. A hump in the middle (central eight bins) of the plot suggests that the spin vector projections of galaxies tend to point towards the center of the chosen co-ordinate system.

The statistics for the θ -distribution of galaxies of SuperclusterS(202-001+0084) is shown in the Table 1. The statistics for the polar angle distribution in this sample shows that the value of chi-square probability ($P(>\chi^2)$) to be 0.0 i.e., 0 (Smaller than the significant level 0.050 i.e., 5.0%). The auto-correlation coefficient ($C/C(\sigma)$) is found to be 11.9 (greater than 1σ limit). The first order Fourier coefficient ($\Delta_{11}/\sigma(\Delta_{11})$) is found to be -0.03 (smaller than 1.5σ the limit). The first order Fourier probability ($P(>(\Delta_1))$) is found to be 0.0 (Smaller than 0.15 i.e., 15%). Except first order fourier coefficient, other statistical

tests suggest an isotropy. Isotropy in the first order fourier coefficient test suggests that the direction of departure from isotropy.

The statistics of the φ -distribution of galaxies of Super cluster S(202-001+0084) is shown in the Table 1. The statistics for the azimuthal angle distribution in this sample shows that the value of chi-square probability ($P(>\chi^2)$) to be 0.0 i.e., 0(Smaller than the significant level 0.050 i.e., 5.0%). The auto-correlation coefficient ($C/C(\sigma)$) is found to be 132.5 (greater than 1σ limit). The first order Fourier coefficient ($\Delta_{11}/\sigma(\Delta_{11})$) is found to be -0.71 (smaller than 1.5σ the limit). The first order Fourier probability ($P(>(\Delta_1))$) is found to be 0.0(Smaller than 0.15 i.e.,15%). Except first order fourier coefficient , other statistical tests suggest an isotropy. Isotropy in the first order fourier coefficient test suggests that the direction of departure from isotropy.

Conclusion

We have studied the preferred alignment of spin vector orientation of 1331SDSSgalaxies of SuperclusterS[202-+001+0084] that have redshift in the range 0.02 to 0.03. We used the method proposed by Flin & Godlowski (1986) in order to compute two-dimensional data to three dimensional galaxy rotation axis (polar & azimuthal angles). We have carried out random simulation by creating 10^7 virtual galaxies and adopting the method proposed by Aryal & Saurer (2000) in order to find theoretical distribution of galaxy rotation axes. We have compared the differences between theoretical distributions and observed distributions using three statistics, namely chi-square, auto-correlation and the Fourier. The distribution of spin vector and spin vector projections of total SDSS galaxies that have redshift in the range 0.02 to 0.03 are found to be random in all samples, our results support Hierarchy model (Peeble, 1969).

However, a local effect that causes the humps and dips in the angular momentum distribution is observed in different samples. In the deep field, density fluctuation is expected and observed in the local scale.

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