# SOIL-PILE-STRUCTURE INTERACTION EFFECTS ON HIGH-RISE BUILDING UNDER SEISMIC SHAKING

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#### **ABSTRACT**

In this paper, study of the response (base shear, time period, storey drift, storey displacement) of a structure is done for the tall building including basement with fixed base and with pile foundation considering Soil Structure Interaction (SSI). Finite element based program ETABS2016 v16.1.0 is used for the analysis of the superstructure. Seismic analysis is done to get the dynamic response of superstructure for two types of model, one model is with fixed baseand second is Model with Winkler spring for Chhaya Center, Thamel, a high rise building with 14 story including double basements. It is observed with the consideration of Soil Structure Interaction (SSI). The soil is replaced by spring and assigned at joints. El Centro earthquake (1940) is used for time history analysis. The response obtained due to SSI effect is compared with fixed based model. Results of analysis presented include the comparison of natural periods, base shears, displacements and overturning moment. It is observed that the natural periods increase and the base shears decrease as the base become more flexible.

#### 1. INTRODUCTION

Structures founded on rock are considered to be fixed base structure. Computation of their response is relatively simple. On the other hand, the same structure would respond differently if supported on soft deposit. First, the inability of the foundation to confirm to the deformations of the free field motion. Second, the dynamic response of the structure itself would induce deformation of the supporting soil. This process, in which the response of the soil influences the motion of the structure and the response of the structure influence the motion of the soil, is referred to as soil structure interaction.

#### 1.1 Types of Analysis

#### 1.1.1 Direct Analysis

Direct Analysis method is the one in which the soil and substructure are modeled together in a single step accounting for both inertial and kinematic interaction. Inertial interaction develops in structure due to own vibrations give rise to base shear and base moment, which in turn cause displacements of the foundation relative to free field. Kinematic interaction develops due to presence of stiff foundation elements on or in soil cause foundation motion to deviate from free field motions.

#### 1.2.2 Substructure Approach

Sub-Structure Method is one in which the analysis is broken down into several steps that

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is the principal of superposition is used to isolate the two primary causes of soilstructure interaction, inability of foundation to match the free field deformation and the effect of dynamic response of structure foundation system on the movement of supporting soil.

#### 1.1 Problem Statement

Conventional structural design methods neglect the SSI effects. Neglecting SSI is reasonable for light structures in relatively stiff soil such as low rise buildings and sample rigid retaining walls. The effect of SSI, however, becomes prominent for heavy structures resting on relatively soft soils for example nuclear power plants, high-rise buildings and elevated-highways on soft soil.

A controversial issue in the seismic analysis and design of high rise building lies in incorporating the effects of the seismic response of these structures. Building codes lack recommendations concerning this controversy; thus, the designers are basing their analysis on approximations, engineering judgment and experience. This has been an active area of research throughout the past decade: (Dutta and Roy, 2002), (Dutta et al., 2004), (Shakib, 2004), (Naim et al., 2008), (El Ganainy and El Naggar, 2009), (Raychowdury 2010), (Tabatabaeifar and Massumi, 2010). The soil-structure interaction (SSI) is a complicated phenomenon for structures coupled with the soil medium, which is generally semi-infinite in extent and nonlinear in its material behavior. The problem of SSI in the seismic analysis of highrise buildings with pile foundation have become increasingly important, as it may be inevitable to build such a structures for the sites with less favorable geotechnical conditions due to ever-increasing difficulty in acquiring new construction sites.

Damage sustained in recent earthquakes, such as the 2015 Gorkha earthquake, 1995 Kobe earthquake, have also highlighted that the seismic behavior of a structure is highly influenced not only by the response of the superstructure, but also by the response of the foundation and the ground as well.

#### 2. LITERATURE REVIEW

Few research has been conducted related to seismic response of high rise building with pile foundation due to soil structure interaction.

Dr. SushmaPulikanthi and Prof. Pradeep Kumar Ramancharla,2013 observed that there is two times increase in the acceleration response of the top floor while considering the SFSI over fixed base analysis for nonlinear case of buildings supported on pile foundation under transient loading.

Kraus & D.dzakic,2013 observed that story drift is increased when the soil is modeled using Winkler springs.

MuberraEserAydemir investigated the seismic behavior of multi storied structures considering SSI according to Turkish Seismic design code and he found that there is

increase in natural period of the structure considering SSI corresponding to rigidly supported structure.

#### 3. METHODOLOGY

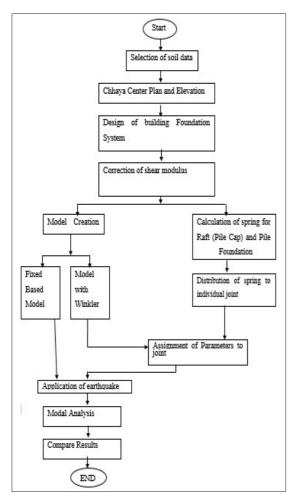


Fig: Flowchart for the methodology

### 3.1 Method Adopted

- Simplified Approach
- Follows Code ASCE 41-06
- Follows Hien Manh Nghiem, "Soil Pile Structure Interaction Effects on high rises under seismic shaking" University of Colorado at Denver and health science, Denver, USA
- The Fixed Support is replaced by one parameter property i.e. Linear Springs

#### 3.2 Steps of SSI Followed

- 1. Calculation of shear modulus
- 2. Calculation of spring stiffness
- 3. Distribution of spring on each joint

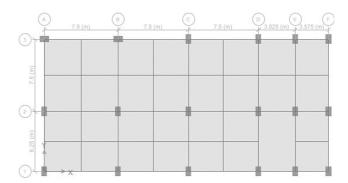


Figure: Typical Plan of Chhaya Center

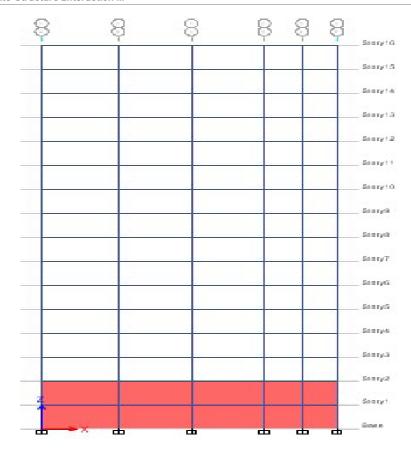


Figure: Typical Elevation of Chhaya Center (16 Story)

## 3.3 Stiffness for Raft Foundation (Pile Cap), Shear wall and Pile Foundation Table: Formula for Calculating Spring Stiffness (ASCE, 2010)

Degree of Freedom	Stiffness of Foundation at surface
Translation along x-axis	$K_x$ , sur = $\frac{GB}{2-v}$ [3.4( $\frac{L}{B}$ ) <sup>0.65</sup> + 1.2]
Translation along y-axis	$K_y$ , sur= $\frac{GB}{2-v}$ [3.4( $\frac{L}{B}$ ) <sup>0.65</sup> + 0.4 $\frac{L}{B}$ + 0.8]
Translation along z-axis	$K_{z}$ , sur = $\frac{GB}{1-v} [1.55(\frac{L}{B})^{0.75} + 0.8]$
Rocking about x-axis	$K_{xx}, sur = \frac{GB^3}{1-v} \left[ 0.4 \left( \frac{L}{B} \right) + 0.1 \right]$
Rocking about y-axis	$K_{yy}$ , sur = $\frac{GB^3}{1-v} [0.47(\frac{L}{B})^{2.4} + 0.034]$
Rocking about z-axis	$K_{zz}$ , sur = $GB^3[0.53(\frac{L}{B})^{2.45} + 0.51]$

**Table:** Formula for Calculating Spring Stiffness (ASCE, 2010)

Degree of Freedom	Correction Factor for Embedment
Translation along x-axis	$\beta = (1+0.21\sqrt{\frac{D}{B}})[1+1.6(\frac{hd(B+L)}{BL^2})^{0.4}]$
Translation along y-axis	$\beta_{y} = (1+0.21\sqrt{\frac{D}{L}})[1+1.6(\frac{hd(B+L)}{BL})^{0.4}]$
Translation along z-axis	$\beta_z = (1 + \frac{1}{21} \frac{D}{B} (2 + 2.6 \frac{B}{L})) [1 + 0.32 (\frac{d(B+L)}{BL})^{\frac{2}{3}}]$
Rocking about x-axis	$\beta_{xx} = 1 + 2.5 \frac{d}{B} \left[ 1 + \frac{2d}{B} \left( \frac{d}{D} \right)^{-0.2} \sqrt{\frac{B}{L}} \right]$
Rocking about y-axis	$\beta_{yy}=1+1.4(\frac{d}{L})^{0.6}[1.5+3.7(\frac{d}{D})^{1.9}(\frac{d}{D})^{-0.6}]$
Rocking about z-axis	$\beta_{zz} = 1 + 2.6 \left( 1 + \frac{B}{L} \right) \left( \frac{d}{B} \right)^{0.9}$

#### 3.4 Stiffness for Pile Foundation

Hien Manh Nghiem, "Soil Pile Structure Interaction Effects on high rises under seismic shaking" University of Colorado at Denver and health science, Denver, USA

#### 3.4.1 Torsional Stiffness

For constant  $K_{qz}$  or  $G_s$ :

$$K_{_{66}}^{^{i}} = \frac{L_{_{e}}(12G_{_{p}}J_{_{p}}k_{_{\partial\!z}} + k_{_{\theta}}^{2}L_{e}^{2}}{4(3G_{_{p}}J_{_{p}} + k_{_{\partial\!z}}L_{e}^{2} + 3k_{_{\partial\!z}}L_{e})} + \frac{K_{_{\partial\!z}b}(3G_{_{p}}J_{_{p}} + k_{_{\theta\!z}}L_{e}^{2}}{(3G_{_{p}}J_{_{p}} + k_{_{\partial\!z}}L_{e}^{2} + 3k_{_{\partial\!z}b}L_{e})} \tag{3-1} \\ \text{Where,}$$

L<sub>e</sub> is the Length of the pile.

G<sub>p</sub> is Pile material shear modulus.

 $J_p$  is polar moment of inertia of pile section.

$$=4\pi^2G\tag{3-1a}$$

$$\mathbf{k}_{\partial b} = \mathbf{r}_0^3 \,\mathbf{G} \tag{3-1b}$$

#### 3.4.2 Vertical Stiffness

For constant K<sub>uz</sub> or E<sub>s</sub>:

$$K_{33}^{i} = \frac{L_{e}(12E_{p}A_{p}k_{uz} + k_{uz}^{2}L_{e}^{2}}{4(3E_{p}A_{p} + k_{uz}L_{e}^{2} + 3k_{uzb}L_{e})} + \frac{K_{uzb}(3E_{p}A_{p} + k_{uz}L_{e}^{2}}{(3E_{p}A_{p} + k_{uz}L_{e}^{2} + 3k_{uzb}L_{e})}$$
(3-2)

Where,

L<sub>a</sub> is the Length of the pile.

 $E_{p}$  is Elastic modulus of pile.

A<sub>p</sub> is Area of Pile.

$$k_{uz} = 2\pi r_0 \frac{G}{r_o \ln\left(\frac{r_m}{r_o}\right)} = 2\pi \frac{G}{\ln\left(\frac{r_m}{r_o}\right)}$$
 (3-2a)

Where.

$$r_m = 2.5 \text{ Lp}(1 - v)$$
 (3-2b)

$$k_{uzb} = \frac{2DG_S}{1-\nu}$$
 (3-2c)

Where,

D is the diameter of the pile.

#### 3.4.3 Lateral Stiffness, Rotation Stiffness and Couple Stiffness

#### 3.4.3.1 Lateral Stiffness

$$k_{11} = \frac{60480EI^{2}k_{uy}L + 1956EIk^{2}_{uy}L^{5} + k^{3}_{uy}L^{9}}{4(15120EI^{2} + 1224EIk_{uy}L^{4} + k^{2}_{uy}L^{8})}$$
(3-3)

#### 3.4.3.2 Rotation Stiffness

$$k_{55} = \frac{1512000EI^{2}k_{uy}L^{3} + 5220EIk^{2}_{uy}L^{7} + k^{3}_{uy}L^{11}}{300(15120EI^{2} + 1224EIk_{uy}L^{4} + k^{2}_{uy}L^{8})}$$
(3-4)

#### **Couple Stiffness**

$$k_{15} = \frac{k_{uy} L^2 + (k^2_{uy} L^8 + 302400EI^2 + 3060EIk_{uy} L^5)}{40 (15120EI^2 + 1224EIk_{uy} L^4 + k^2_{uy} L^8)}$$
(3-5)

Where.

L<sub>e</sub> is the Length of the pile.

E<sub>p</sub> is Elastic modulus of pile.

A<sub>p</sub> is Area of Pile.

$$I = \frac{1}{4}\pi r^4$$

$$K_{uy} = \frac{0.65 \, E_S}{1 - {}^{V}S^2} \left(\frac{E_S D^4}{EI}\right)^{\frac{1}{12}} \tag{3-5a}$$

Where,

D is the diameter of the pile.

Again,

$$K_{11} = \frac{k_{14}^2 k_{33} - 2k_{13} k_{14} k_{34} + k_{13}^2 k_{44}}{k_{24}^2 - k_{23} k_{44}} + k_{11}$$
 (3-5b)

$$K_{55} = \frac{k_{24}^2 k_{33} - 2k_{23} k_{24} k_{34} + k_{23}^2 k_{44}}{k_{34}^2 - k_{33} k_{44}} + k_{22}$$
 (3-5c)

$$K_{15} = \frac{k_{24}^{2}(k_{24}k_{33} - k_{23}k_{24}) + k_{13}(k_{23}k_{44} - k_{24}k_{34})}{k_{34}^{2} - k_{33}k_{44}} + k_{12}$$
(3-5d)

Where,

$$k_{11} = \frac{EI}{I^3} \left( 12 + \frac{13}{35} A \right) \tag{3-5e}$$

$$k_{12} = \frac{EI}{L^2} \left( 6 + \frac{11}{210} A \right)$$
 (3-5f)

$$k_{13} = \frac{EI}{L^3} \left( -12 + \frac{9}{70} A \right)$$
 (3-5g)

$$k_{14} = \frac{EI}{L^2} \left( 6 - \frac{13}{420} A \right) \tag{3-5h}$$

$$k_{22} = \frac{EI}{L} \left( 4 + \frac{1}{105} A \right) \tag{3-5i}$$

$$k_{23} = \frac{EI}{L^2} \left( -6 + \frac{13}{420} A \right)$$
 (3-5j)

$$k_{24} = \frac{EI}{L} \left( 2 + \frac{1}{140} A \right)$$
 (3-5k)

$$k_{33} = \frac{EI}{L^3} \left( 12 + \frac{13}{35} A \right) + \overline{K}_{11};$$
 (3-51)

$$k_{34} = \frac{EI}{L^2} \left( -6 - \frac{11}{210} A \right) + \overline{K}_{15}$$
 (3-5m)

$$k_{44} = \frac{EI}{L} \left( 4 + \frac{1}{105} A \right) + \overline{K}_{55}$$
 (3-5n)

And 
$$A = \frac{k_{uy} L^4}{EI}$$
 (3-50)

Where  $\overline{K}_{11}$ ,  $\overline{K}_{55}$ , and  $\overline{K}_{15}$  are equivalent lateral, rotation and couple stiffness of lower pile segments located at the current pile segment.

#### 4. CALCULATION

Details of soil profile in site obtained from lab and insitu test are shown in table 1 which are used in SSI.

Table 1: Details of soil properties

Depth (m)	Thickness (m)	Soil Type		N		Vs(f)	Vs(Cor)	ρ(g/cm³)
0-2	2	Silty clay	18.69	9	14	172.143	261.810	1.35
2-6	4	Silty sand	60.045	31	35	215.593	244.915	1.46
6-9	3	Clay	87.615	29	27	202.092	208.883	1.46
9-10.5	1.5	Sand	101.4	71	65	252.08	251.205	1.46
10.5-13.5	3	Sand	128.97	50	40	223.767	209.978	1.47
13.5-15	1.5	Silty sand	142.755	50	38	220.911	202.102	1.47

Where,

$$Vs(f)=87.8$$
 [Brandenberg et al. (2010)] (4.3a) and,

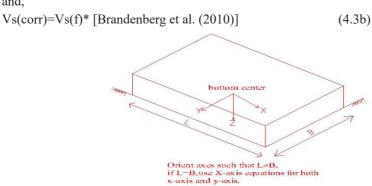
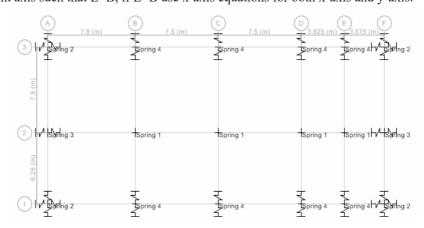


Figure 44: Raft Foundation Plan

Orient axis such that L>B, if L=B use x-axis equations for both x-axis and y-axis.



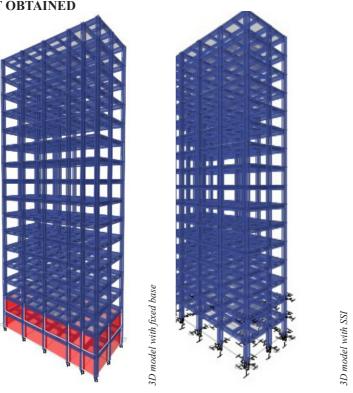
The calculated parameters of damping and springs are individual parameters acting at a defined direction. However, the assignment of the spring and dashpot occur in group.In ETABS, more than two springs cannot be assigned to a single joint. Hence, a group of individual parameter are combined to form a single joint. i.e. joint S1, S2, S3, S4, S5, S6

and S7 are the set of individual spring parameters k1, k2, k3, k4, k5, k6.

**Table**: Spring Distribution

Parameter				Spring Typ	e		
1 at attricted	S1 S2	S2	S3	S4	S5	S6	S7
Spring	k3	k1, k2, k3, k4, k5	k1, k3, k4	k2, k3, k5	k1,k4	k2,k5	k1, k2, k4, k5

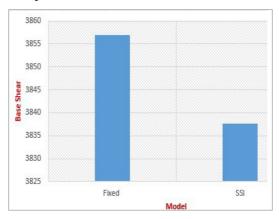
## 5. RESULT OBTAINED



## **5.1 Comparison of Output-Time Period**

Mode	Fixed	SSI	5							- 2						3	
Mode 1	2.515	2.54	4.5														
Mode 2	2.291	2.318	4	-	-											2.5	
Mode 3	2.028	2.04	3.5 S			1										2	
Mode 4	0.791	0.795	S) 3			1											
Mode 5	0.737	0.741	2.5	-												1.5	
Mode 6	0.645	0.646	2.5 2 2.5 1.5			1	1									1	——Fixed
Mode 7	0.433	0.435	E 1.5				1	-	-								SSI
Mode 8	0.417	0.419	0.5				_	_	_	>	-	-				0.5	
Mode 9	0.356	0.357	0.5												=	0	
Mode 10	0.284	0.286		le 1	le 2	9	e 4	le 5	9 e	le 7	e 90	6 a	10	1	12		
Mode 11	0.282	0.284		Mode 1	Mode 2	Mode 3	Mode 4	Mode	Mode 6	Mode 7	Mode 8	Mode 9	Mode 10	Mode 11	Mode 12		
Mode 12	0.233	0.234							Mo	ode			2	-	~		

### 5.2 Comparison of Output-Base Shear

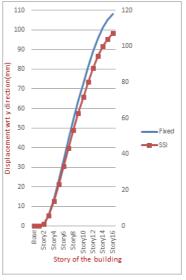


## 5.3 Comparison of output-Displacement w.r.t. x

	Displacement	Displacement	90 —	100
Story	w.r.t. x for	w.r.t. x for		
Story	fixed case	SSI case	80 ————	90
	(mm)	(mm)		/ /
Base	0	0	<del>2</del> 70 ———————————————————————————————————	80
Story1	0.11	0.172	O is pal coment wat x direction (aum) 20 Spal coment wat x direction (aum) 30 Spal coment wat x direction (aum) 40 Spal co	70
Story2	0.318	0.817	5 60 J	
Story3	4.815	5.075	D //	60
Story4	12.074	12.204	₩ 50	
Story5	20.058	20.031	# 40	50
Story6	28.464	28.263	#U #U	40 Fixed
Story7	36.836	36.502	8 30	→ SSI
Story8	45.032	44.565	<u> </u>	30
Story9	52.93	52.337	20	
Story10	60.41	59.699		20
Story11	67.34	66.527	10	10
Story12	73.582	72.688	<i>,</i>	
Story13	78.993	78.041	0 +++	0
Story14	83.428	82.45	ene story total story of the	Ay Ay Ay
Story15	86.772	85.802	* 55. 55. 55. 55. 50. 5	b. 20, 20,
Story16	89.066	88.136	Story of the bu	ilding

## 5.4 Comparison of output-Displacement w.r.t. y

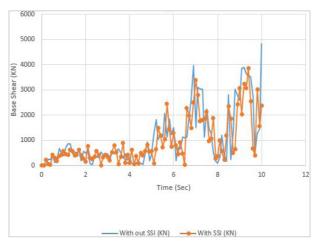
	Displacement	Displacement
Story	w.r.t. y for	w.r.t. y for
Story	fixed case	SSI case
	(mm)	(mm)
Base	0	0
Story1	0.208	0.097
Story2	0.749	0.982
Story3	5.591	5.682
Story4	13.866	13.786
Story5	23.469	23.224
Story6	33.676	33.268
Story7	43.95	43.384
Story8	54.036	53.32
Story9	63.751	62.899
Story10	72.932	71.96
Story11	81.416	80.345
Story12	89.035	87.893
Story13	95.624	94.441
Story14	101.035	99.85
Story15	105.194	104.045
Story16	108.241	107.163



#### 5.5 Comparison of Output-Overturning Moment

Story	Fixed Base (mm)	Winkler approach considering SSI (mm)	2500																		
Base	2036.112	1342.597																			
Story1	1853.323	1342.309	2000	-																	
Story2	1673.221	1370.336	ē		1																
Story3	1496.792	1344.868	Moment 1500			1															
Story4	1325.277	1189.447																			
Story5	1159.104	1037.755	1000																		
Story6	998.8839	890.4173	E 1000						/												——Fixed
Story7	846.1835	750.0687	=						-	-	1										I IXEU
Story8	701.8881	618.5974	o 500																		-SSI
Story9	565.5118	495.7521	O 500																		
Story10	438.1567	383.1397																			
Story11	324.4241	286.4841															-				
Story12	228.1264	208.4841	0		_	O.	m	-	10	10	_	m	0	0	-	O.I	m	**	2	10	1
Story13	147.1475	141.9164		Base	Story1	Story2	Story3	7	7	2	7	7	Ston/9	710	y1:	71	77	77	71	716	
Story14	77.8231	79.1684		- 60	Sto	Stc	Stc	Stc	Stc	Story6	Stc	Stc	Stc	Story1	Story1	Story12	Stony1	Story1	Story1	Story16	
Story15	24.4523	26.0304														S	S	S	S	S	
Story16	0	0							S	tory	of	the	bui	ldin	g						

## 5.6 Comparison of Output-Base Shear w.r.t Time History of El Centro Earthquake (1940)



#### 6. CONCLUSION

- The soil structure interaction effects increase the time period of the structure.
- It was observed that the base shear decreases in SSI based Winkler approach
  model than fixed based model as the base becomes more flexible by the
  inclusion of SSI effects.
- It was observed that the displacement decreases in SSI based Winkler approach model than fixed based model.
  - Overturning moment is decreased in SSI based Winkler approach model than fixed based model.

Base shear is increased in some time and decreased in rest while analyzing the model with time history of El Centro earthquake between fixed and SSI cases.<sup>2</sup>

<sup>1.</sup> ASCE (2007), Seismic Rehabilitation of Existing Buildings, ASCE/SEI 41-06, American Society of Civil Engineers, Reston, Virginia.

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