# MOBILE WHEELED ROBOT MOTION CONTROL WITH USAGE OF GEOLOCATION SENSORS 

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#### Abstract

The authors state mobile robot motion control peculiarities which are induced by geolocation sensors operation. This paper specifies features of geolocation sensors - GPS receiver and electronic compass (magnetometer). Lay of land and man-made structures are obstacles for GPS signals. The paper describes precision of GPS receiver and offers a method that can reduce probable error of GPS signal. This method is a program digital filter based on finding of GPS data kernel - most likely mobile robot location which is expressed in terms of latitude and longitude. The paper formulates functioning principles of the six-wheeled robot movement automatic control system that uses geolocation sensors data.


Key words: mobile robot, control system, robotics, geolocation, GPS, magnetometer.

## INTRODUCTION

During the last two decades, automatic control of wheeled mobile objects movement is actual objective due to a wheeled mover became the most widespread and this mover type has the greatest coefficient of efficiency. Many papers, written by authors: D.E. Ohocimsky, E.A. Devyanin, Ju. G. Martynenko, V.E. Pavlovsky, A.M. Formalsky, S.F. Yatsun, A.P. Krischenko, S.B. Tkachev, M.L. Zymbler, T. Bretl and their apprentices, describe methods of mobile wheeled robot control under determined and non-determined conditions of environment [1, 2]. In addition to previously mentioned, special attention is paid to control of robot powered with electrical motors. The wheel-motor unit is a device containing wheel, electrical drive, transmission, and braking system. Generally, this unit is mounted by underslung cantilever on chassis frame. Nowadays, such devices are used in electric car and mobile robot designs.

## MATERIALS AND METHODS

The mobile six-wheeled robot "X6WD" (Fig. 1) was designed in Southwest State University for development and research of mobile object control methods with usage of geolocation. This robot design is based on chassis frame with six wheel-motors. The robot "X6WD" has onboard control system, autonomous power supply unit, geolocation sensors - GPS receiver "Seeed Studio GPS-Bee" (Fig. 2) and three-axis magnetometer "Devantech CMPS10" (Fig. 3), video camera, two manipulators with 5 degrees of freedom, and lighting equipment
[3]. The robot overall dimensions (with maximum elongate manipulators): $780 \mathrm{~mm} \times 305 \mathrm{~mm}$ x 340 mm , its mass -6 kg , its maximum linear velocity at movement on even surface - 14 $\mathrm{km} / \mathrm{h}$. The robot control system based on client-server model: the robot is a server controlled by client - remote computer via Internet or wireless LAN [4] (Fig. 4).


Figure 1 The X6WD mobile six-wheeled robot


Figure 2 The Seeed Studio GPS-Bee GPS receiver


Figure 3 The Devantech CMPS10 magnetometer


Figure 4 Chart of the robot control system
The CMPS 10 module determines the bearing - the angle $\varphi$ between the robot body forward direction and the direction from robot body to magnetic north (Fig. 5). The CMPS10 produces the bearing in the range from -179 to +180 degrees. The CMPS10 includes threeaxis magnetometer and three-axis accelerometer that allows compensating the bearing error induced by tilting of the CMPS10 module. In addition to previously mentioned, built-in accelerometer gives information about roll and trim angles of robot body. The minimal determined bearing value by CMPS10 module is 0.1 degree. The roll and trim values range from -60 to +60 degrees. Communication between the CMPS10 module and the onboard control system of robot is carried out by serial interface $I^{2} \mathrm{C}$.


Figure 5 The bearing $\varphi$

The GPS receiver "Seeed Studio GPS-Bee" is based on U-Blox Neo-5 microcircuit. It has following parameters: maximum number of channels (GPS satellites) - 50, inaccuracy of position determination $- \pm 1.017 \mathrm{~m} . . \pm 30.33 \mathrm{~m}$, position updating duration - less than 1 sec , communication bus between the GPS receiver and the onboard control system of robot serial interface UART.
To provide the robot movement control process we need to convert spherical coordinates of the Earth (longitude and latitude) into rectangular coordinates $-x$ and $y$ (Fig. 6):

$$
\begin{align*}
& x=\Lambda \cdot R_{1},  \tag{1}\\
& y=\Phi \cdot R_{2}, \tag{2}
\end{align*}
$$

where: $\Lambda$ - longitude $(-\pi \leq \Lambda \leq \pi \mathrm{rad})$, $\Phi$ - latitude $(-\pi / 2 \leq \Phi \leq \pi / 2 \mathrm{rad})$, $R_{1}=6378.16 \mathrm{~km}$ (Equatorial radius), $R_{2}=6356.77 \mathrm{~km}$ (Polar radius).


Figure 6 Spherical coordinates of the Earth

The inaccuracy of bearing $\varphi_{i}$ determination can be denoted by $\Delta \varphi$. Thus, during robot movement to a destination point the robot body executes process of rotation so that the bearing value could be $\varphi_{i} \pm \Delta \varphi$, where $\varphi_{i}$ is calculated on the basis of current coordinates ( $x_{C}$ and $y_{C}$ ) of the robot body and coordinates ( $x_{i}$ and $y_{i}$ ) of a destination point [5]:

$$
\varphi_{i}=\left\{\begin{array}{l}
{\left[\frac{\pi}{2}-\left[\arccos \left[\frac{x_{i}-x_{C}}{\left[\sqrt{\left(x_{i}-x_{C}\right)^{2}+\left(y_{i}-y_{C}\right)^{2}}\right]}\right]\right]\right], \text { if }\left(y_{i}-y_{C}\right) \geq 0,}  \tag{3}\\
{\left[\pi \cdot \operatorname{sign}\left(x_{i}-x_{C}\right)+\left[\frac{\pi}{2}-\left[\arccos \left[\frac{x_{i}-x_{C}}{\left[\sqrt{\left(x_{i}-x_{C}\right)^{2}+\left(y_{i}-y_{C}\right)^{2}}\right] \cdot \operatorname{sign}\left(x_{i}-x_{C}\right)}\right]\right]\right] \cdot\left(-\operatorname{sign}\left(x_{i}-x_{C}\right)\right)\right], \text { if }\left(y_{i}-y_{C}\right)<0,}
\end{array}\right.
$$

where sign is the signum function:

$$
\operatorname{sign}(x)=\left\{\begin{array}{lll}
1, & \text { if } & x \geq 0,  \tag{4}\\
-1, & \text { if } & x<0 .
\end{array}\right.
$$

Thereby, $\varphi_{i} \in(-\pi, \pi]$. Sign of the bearing $\varphi_{i}$ means a destination point location: at $\varphi_{i}<0$ destination point is located in the west, at $\varphi_{i}>0-\mathrm{it}$ is located in the east.
The course deviation is a difference between the specified bearing $\varphi_{i}$ and the current bearing $\varphi_{C}$ :

$$
\begin{equation*}
\Theta=\varphi_{i}-\varphi_{C}, \tag{5}
\end{equation*}
$$

in this connection:

$$
\begin{align*}
& \text { if } \Theta>\pi \text {, then } \Theta=-(2 \pi-\Theta),  \tag{6}\\
& \text { if } \Theta \leq-\pi \text {, then } \Theta=2 \pi+\Theta, \\
& \Theta \in(-\pi, \pi] .
\end{align*}
$$

After course deviation calculation there are possible the following variants of robot movement:

- if $|\Theta|>\Delta \varphi$ and $\Theta>0$, then the robot body turns to right (clockwise rotation);
- if $|\Theta|>\Delta \varphi$ and $\Theta<0$, then the robot body turns to left (contraclockwise rotation);
- if $|\Theta| \leq \Delta \varphi$, then the robot body does not turn, i.e. there is possible straightforward movement of the robot.
The criterion of robot movement completion can be denoted by following equations:

$$
\begin{align*}
\left|x_{i}-x_{C}\right| & =\Delta x,  \tag{7}\\
\left|y_{i}-y_{C}\right| & =\Delta y, \\
\left|\varphi_{i}-\varphi_{C}\right| & =\Delta \varphi,
\end{align*}
$$

where:

- $x_{i}, y_{i}$ and $\varphi_{i}$ are destination point coordinates and specified bearing;
- $x_{C}, y_{C}$ and $\varphi_{C}$ are current robot body coordinates and bearing;
- $\Delta x, \Delta y$, and $\Delta \varphi$ are determination inaccuracies of coordinates $x, y$ (induced by GPS receiver bias and obstacles for GPS signals), and bearing $\varphi$ (induced by magnetometer and intense magnetic fields), respectively.

Generally, the $\Delta x$ and $\Delta y$ values are induced by lay of land and man-made structures which are obstacles for GPS signals. In many cases the $\Delta x$ and $\Delta y$ inaccuracies are independent and different values (Fig. 7).


Figure 7 The $\Delta x$ and $\Delta y$ inaccuracies
The program digital filter "Constellation" is the method that can reduce probable error of GPS signal and help to decrease the $\Delta x$ and $\Delta y$ values. This program filter is based on finding of the GPS data kernel - most likely mobile robot location which is expressed in terms of latitude and longitude. The GPS data kernel is formed from two neighboring points of latitude or longitude. First of all the main advantage of the filter "Constellation" is its algorithm simplicity and high calculating speed. Moreover, the filter does its function in consideration of previous filtered values. The filter can be realized on basis of a personal computer or a microcontroller, such as Atmel ATmega32U4 or NXP Semiconductors LPC2880. The filter "Constellation" is a program class written in $\mathrm{C}++$ language.

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The filter class has following members - member functions (methods) and member variables:

```
class TConstellation
{
private: // keyword "private" sets accessibility of
    double Buf[N];
    unsigned int BufCounter; // the counter for calculation of buffer filling;
    double Mean; // the variable stores filtered value of
    // latitude/longitude;
    double ED[(N-1)* N][3]; // the array for data kernel search;
    // keyword "public" sets accessibility of
    // the class members for all program objects;
    double Buffer(int index); // the method returns one latitude/longitude
    // sample that is conformable to its index;
    int MaxIndex(void); // the method returns maximum value of
    // sample index within buffer size;
    double Filter(void); // the method allows to filter
    // latitude/longitude samples;
    double Average(void); // the method returns arithmetic mean value of
    // latitude/longitude samples;
    void Add(double S); // the method allows to add one
    // latitude/longitude sample to the buffer;
    TConstellation(void);// the constructor method allows to initialize
    // the class member variables.
};
```

The value of N is a maximum amount of latitude or longitude samples which are stored in the buffer "Buf". In many cases the value of $\mathrm{N}=20$ is sufficient ( $\mathrm{N} \geq 3$ ). If the class methods "Buffer", "Filter", and "Average" fail, they return -1. The buffer "Buf" must be filled by the method "Add" before using the method "Filter".
The text of program module "Constel.cpp" with implementation of the class methods is presented below.

```
#pragma hdrstop
#include <math.h>
#include "Constel.h"
double TConstellation::Buffer(int index)
{f (index < BufCounter) return Buf[index]; else return -1;
int TConstellation::MaxIndex(void)
if (BufCounter < N) return (BufCounter - 1); else
return (N - 1);
}
```

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/////////////////////////////////////////////////////////////////////////

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```
doub7e TConstel1ation::Filter(void)
{
unsigned int h = 0;
unsigned int k = 0;
unsigned int d = 0;
unsigned int m = 0;
unsigned int minED = 0;
unsigned int proxE1 = 0;
unsigned int proxE2 = 0;
    if (BufCounter > 2)
    for (h = 0; h <= BufCounter - 1; h++)
        {for (k = 0; k <= BufCounter - 1; k++)
            {
                if (h != k)
                        ED[d][0] = fabs(Buf[h] - Buf[k]);
                ED[d][1] = h;
                d++;
                }
        }
    }
        for (m = 1; m <= d - 1; m++)
        if (ED[minED][0] >= ED[m][0]) minED = m; //GPS data kerne1 search
    }
        d = 0;
        proxE1 = ED[minED][1];
        proxE2 = ED[minED][2];
        minED = 0;
        if (BufCounter <= N) Mean = (Buf[proxE1] + Buf[proxE2]) / 2;
        else
        if (fabs(Mean - ((Buf[proxE1] + Buf[proxE2]) / 2)) >= fabs(Buf[proxE1] -
        - Buf[proxe2]))
        Mean = (Buf[proxE1] + Buf[proxE2]) / 2;
        }
    }
    else
    {
        if (BufCounter > 1) Mean = (Buf[0] + Buf[1]) / 2; else
        if (BufCounter > 0) Mean = Buf[0]; else Mean = -1;
    }
```

return Mean;
${ }_{3}$
///////////////////////////////////////////////////////////////////////////
double TConstellation::Average(void)
\{
double $A=0$;
if (BufCounter $>0$ )
for (int $\mathbf{i}=0 ; i<B u f C o u n t e r ; i++$ ) $A=A+B u f[i] ;$
return A / BufCounter;
\}
else return -1 ;
\}
void TConstellation::Add(double s)
\{

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```
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if (BufCounter < N)
        Buf[BufCounter] = s;
        BufCounter++;
    }
    else
        for (int i = 0; i < N - 1; i++) Buf[i] = Buf[i + 1];
        Buf[N - 1] = s;
    }
}
```

///////////////////////////////////////////////////////////////////////////////////
TConstellation::TConstellation(void)
$\{$
Bufcounter $=0$;

for (int $\mathbf{i}=0$; $\mathbf{i}<(N-1) * N ; i++$ ) \{ $\operatorname{ED[i][0]~=0;~ED[i][1]~=~0;~ED[i][2]~=~0;~\} ~}$ Mean $=0$; \}
///////////////////////////////////////////////////////////////////////////////////1/2l

## RESULTS AND DISCUSSION

The series of GPS measurements was carried out using the Seeed Studio GPS-Bee receiver mounted on the X6WD robot. The measurements results give the information about the lay of land and man-made structures influences on the $\Delta x$ and $\Delta y$ inaccuracies. Also, the results allow estimating the dispersion of latitude/longitude samples under certain environmental conditions. To obtain the precise latitude/longitude, the value the GPS data samples is filtered by the program digital filter "Constellation", and then filtered GPS data is used in the calculation of latitude/longitude arithmetic mean value. This method gives maximum accurate measurements results. Therefore it is possible to evaluate the probability of certain latitude/longitude sample occurrence. This probability can be evaluated in relation to the latitude/longitude arithmetic mean. Thus, a perfect or partial coincidence between the maximum probability value and the arithmetic mean is possible at the robot location without any obstacles for GPS signals.

The results of four experiments are presented in the figures $8-23$ and the tables $1-2$ : -1 . The robot is in the building (Fig. $8-11$ ) - this location is characterized as the worst to receive the GPS signals (the signals can penetrate through windows of the building);

- 2. The robot is situated in open territory (Fig. 12-15) - the GPS signals reach the robot easily;
- 3. The robot is in the wreck of the old factory (Fig. 16-19) - this location is bad to receive the GPS signals (the signals can penetrate through breaches of the old factory roof);
- 4. The robot is situated in open territory (Fig. 20-23) - the GPS signals reach the robot easily.
The figures $8,12,16$, and 20 show the dispersion of GPS data samples and their arithmetic mean values. All latitude and longitude values are represented in degrees. The figures 9, 13, 17, and 21 display the probabilities of certain longitude samples occurrence. The figures 10 , 14,18 , and 22 show the probabilities of certain latitude samples occurrence. The figures 11 , 15,19 , and 23 display the Google Maps fragments with the marked points of the robot location. Latitude and longitude values (in degrees) must be calculated with an accuracy of seven decimal places.
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Table 1 - The arithmetic mean values and the most probable values of GPS data samples

| Experiment number | Arithmetic mean of <br> latitude <br> (in degrees) | Arithmetic mean of <br> longitude <br> (in degrees) | Latitude value with <br> maximum probability <br> of occurrence <br> (in degrees) | Longitude value with <br> maximum probability <br> of occurrence <br> (in degrees) |
| :---: | :--- | :--- | :--- | :--- |
| 1 | 51.73906727 | 36.1479643 | 51.73901333 | 36.14763667 |
| 2 | 51.75576472 | 36.1249951 | 51.7558 | $36.12497667 /$ <br> 3 |
| 3 | 51.73137722 | 36.27089615 | $51.73135833 /$ | 36.27093333 |
| 4 | 51.73167356 | 36.27092638 | 51.731675 | 36.270925 |

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Table 1 - The arithmetic mean values and the most probable values of GPS data samples

Table 2 - The maximum dispersions and the inaccuracies of GPS data

| Experiment number | Maximum dispersion <br> of latitude samples <br> (in degrees) | Maximum dispersion <br> of longitude samples <br> (in degrees) | Maximum inaccuracy <br> $\Delta y$ <br> (in metres) | Maximum inaccuracy <br> $\Delta x$ <br> (in metres) |
| :---: | :--- | :--- | :--- | :--- |
| 1 | 0.00022167 | 0.000545 | $\pm 12.29657776$ | $\pm 30.33467063$ |
| 2 | 0.00019 | 0.000065 | $\pm 10.5399238$ | $\pm 3.6178965$ |
| 3 | 0.00015167 | 0.0002 | $\pm 8.41344794$ | $\pm 11.13198922$ |
| 4 | 0.00001833 | 0.00001833 | $\pm 1.01701019$ | $\pm 1.02043235$ |


$\quad$ 믈 Filtered GPS data
ner Arithmetic mean value of GPS data
Figure 8 The dispersion of GPS data samples and their arithmetic mean value

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$n$ Arithmetic mean value of longitude
$\Psi$ Probability of certain longitude value
Figure 9 The probabilities of certain longitude samples occurrence


Figure 10 The probabilities of certain latitude samples occurrence


Figure 11 The Google Maps fragment with the marked point of the robot location - the robot is situated by a window of the building


Foltered GPS data
-n. Arithmetic mean value of GPS data
Figure 12 The dispersion of GPS data samples and their arithmetic mean value

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Figure 13 The probabilities of certain longitude samples occurrence


Figure 14 The probabilities of certain latitude samples occurrence

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Figure 15 The Google Maps fragment with the marked point of the robot location - the robot is situated in open territory


- Filtered GPS data
ner Arithmetic mean value of GPS data
Figure 16 The dispersion of GPS data samples and their arithmetic mean value

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n Arithmetic mean value of longitude
$\Psi$ Probability of certain longitude value
Figure 17 The probabilities of certain longitude samples occurrence


Figure 18 The probabilities of certain latitude samples occurrence


Figure 19 The Google Maps fragment with the marked point of the robot location - the robot is situated under a breach of the old factory roof

a Filtered GPS data
-n Arithmetic mean value of GPS data
Figure 20 The dispersion of GPS data samples and their arithmetic mean value

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n Arithmetic mean value of longitude
$\Psi$ Probability of certain longitude value
Figure 21 The probabilities of certain longitude samples occurrence


п Arithmetic mean value of latitude
$\Psi$ Probability of certain latitude value
Figure 22 The probabilities of certain latitude samples occurrence


Figure 23 The Google Maps fragment with the marked point of the robot location - the robot is situated in open territory

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