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Diffusion of fructose in water: a molecular dynamics study

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Abstract: Present work carries the molecular dynamics (MD) simulation to study the self-diffusion coefficients of fructose ($C_6H_{12}O_6$) and SPC/E (Extended Simple Point Charge) water (H_2O) along with their binary diffusion coefficients at different temperature (298.15 K, 303.15 K, 308.15 K and 312.15 K). A dilute solution of 3 molecules of fructose (solute, mole fraction 0.0018) and 1624 molecules of water (solvent, mole fraction 0.9982) has been taken for making it relevent to the previously reported experiment. The structural analysis of the mixture has been estimated by using the radial distribution function (RDF) of its constituents. Mean square displacement (MSD) and Einstein's relation have been used to find the self-diffusion coefficients of both the solute and solvent. Furthermore, Darken's relation finds the binary diffusion coefficients. The temperature dependence of diffusion coefficients follows the Arrhenius behaviour which further calculates activation energy of diffusion. The results from the present work agree well with the previously reported experimental values.

Keywords: Fructose ● Diffusion coefficient ● Molecular dynamics ● RDF ● Arrhenius behavior

1.   Introduction

Fructose is a simple sugar (monosaccharides) found in many foods and one of the three most important blood sugars along with glucose and galactose[1]. Fructose is a monosaccharide isomer with the same empirical formula as glucose ($C_6H_{12}O_6$) but with different structure[1].

Its IUPAC name is 1,3,4,5,6 - Pentahydroxy - 2 - hexanone and chemical formula is $C_6H_{12}O_6$[2]. Fructose is the sweetest among all other sugar[2]. Fructose is odorless and colorless substance found in white, crystalline or granular powder form[3]. The fructose has a molar mass of 180.159 mol/g and density in solid crystalline form is 1.60 g/cm^3 [4]. It has melting point of 103°C[5]. Fructose has higher solubility than other sugar and refined crystallised fructose appears white in color. Fructose produces clear colorless liquid in water[6] and has a solubility of 4 g per gram H_2O at 25°C[4].

Fructose has been a part of the human diet for many thousand of years which is found in highest concentrations in fruits and to a lesser degree in vegetables[7]. Basically, fructose is the fruit sugar and more

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sweeter than glucose and sucrose. Cane, beet and corn sugars are produced industrially and their use result in significant quantities of added sugar in our diet, about half of which is fructose[7]. It is commonly used as sweetening agent along with glucose under the name High Fructose Corn Syrup (HFCS) for soft drinks. Cells process fructose to extract energy through a process called aerobic respiration, which essentially means burning of fructose in presence of oxygen to produce ATP, the cellular energy molecule. Hence, like glucose, fructose is a source of energy for the cells[8]. The fructose is stored as glycogen by liver cell which can be later broken down by liver to release glucose into the blood stream for use by all body cells[8]. Thus, fructose also helps to maintain blood sugar level. Fructose is essential for spermatozoa metabolism and spermatozoa mobility[9]. Fructose, in semen, is the source of energy of every sperm activites[10]. Thus, fructose is one of the important monosaccharide for living organism. The intake of soft drinks containing High Fructose Corn Syrup (HFCS) can cause obesity. The dietary fructose is potential risk factor for cardiovascular diseases. Study shows that eating diet high in fructose consistently causes hyperlipidemia in rodents, dogs and non-human primates[11]. Excessive consumption of fructose leads to insulin resistance, obesity, cardiovascular diseases etc[12].
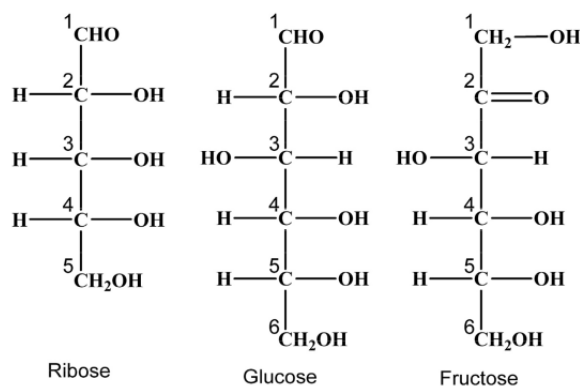
Figure 1.   Structure of monosaccharides [13].

The computer simulation is the ever growing virtual method for observing the interacting particles. This method is used widely everywhere in the world due to its cost effectiveness. Computer simulation has vital role in providing the exact results for many problems in statistical method which were only soluble by approximate method. The strongest aspect of computer simulation is that its result can be compared and analyzed with experimental results by bridging various analogous method. There are two often used computer simulation techniques : Monte Carlo method and Molecular Dynamics (MD) simulation[14]. Monte Carlo method is widely used for structural representations of molecule such as hardspheres and disks whereas Molecular Dynamics is used to explain the solution of classical equation of motion (Newton's Equation). MD describes structural as well as time evolution of the system[14]. The MD simulation is used to study the transport properties of various biomolecules, structure and dynamics of protein, protein folding, docking of protein, first and second order phase transition etc[15]. There are wide range of usages of MD simulation.

Diffusion is the process in which matter is transported from one part to another due to random molecular motion[16]. It is one of the most important biochemical phenomena to occur in nature. It is responsible for transport and exchange of important gases, minerals and nutrients in all living beings. Diffusion process is important for the kinetics of many microstructural changes that occur during preparation, processing and heat treatment of materials which include nucleation of new phases, diffusive phase transformations, homogenization of alloys, recrystallization etc[17]. The applications of diffusion include prcocess such as doping during fabrication of microelectronic devices, operation of solid electrolytes for batteries and fuel cells, surface hardening of steel through carburization or nitridation, diffusion bonding and sintering[17].

The first attempt to measure self-diffusion (the most basic diffusion process) was that of physico-chemist Georg Karl Von Hevesy who studied self diffusion in liquid and in solid lead by using a natural radioisotope ^{210}Pb and ^{212}Pb of lead. From the pioneering work of Alder and Wainwright the simulation of diffusion coefficient has been an area of continuous research. The equations of Fick, the statistical interpretation of diffusion coefficient by Einstein and Smoluchowski and the Boltzmann-Matano method for concentration dependent diffusion coefficients opened the way for experimental techniques[18].

After the introduction part, we describe about the theory of diffusion, modeling of system and simulation procedure, results and dicussion, and conlcusions in order.

2. Methodology

Diffusion Coefficient

Diffusion is a transport phenomenon which occurs due to the presence of concentration gradient[19]. The transport of mass takes place from higher chemical potential region to the lower chemical potential region till the steady state is achieved[20]. Diffusion is a response property of the system to a concentration inhomogeneity[21]. Self-diffusion is the diffusion in absence of a chemical potential gradient in homogeneous medium and corresponding diffusion coefficient is called self-diffusion coefficient[22]. The self-diffusion coefficient is usually calculated by Einstein's relation using mean square displacement (MSD) plot against time (t) and by Green-Kubo's relation using velocity autocorrelation function (VACF). The Einstein's relation to calculate self-diffusion coefficient is given by[23]

$$D = \lim_{t \to \infty} \frac{\langle \mathbf{r}^2(t) \rangle}{6\,t} \tag{1}$$

where D is self-diffusion coefficient, $\langle \mathbf{r}^2(t) \rangle$ is the mean square displacement and t is time.
The Einstein's relation for 3-D system is given as[14, 21]

$$D = \lim_{t \to \infty} \frac{\langle [\mathbf{r}_\alpha(t + t_0) - \mathbf{r}_\alpha(t_0)]^2 \rangle}{6\,t} \tag{2}$$

where α denotes the type of component (solute or solvent) and t_0 is any time origin. The angled brackets $\langle \ldots \rangle$ indicate the ensemble average. The ensemble average is taken over all atoms of the component α in the simulation

and all time origins [22, 24].

In the present work, we calculate the self-diffusion coefficients of fructose (solute) and water (solvent) using Einstein's relation and thus, calculated self-diffusion coefficients are used to estimate binary diffusion coefficient using Darken's relation[25]

$$D_{12} = N_2 D_1 + N_1 D_2 \tag{3}$$

where D_{12} is binary diffusion coefficient, D_1 and D_2 are the self-diffusion coefficients of molecules 1 and 2 respectively and N_1 and N_2 are the corresponding mole fractions.

Modeling of the system

We have carried out molecular dynamics simulation in **GRO**ningen **MA**chine for **C**hemical **S**imulation (**GROMACS**) **5.1.1** package using OPLS/AA force field. The system consists of 3 molecules of fructose and 1624 SPC/E water molecules. The simulation has been carried out at four temperatures i.e. 298.15 K, 303.15 K, 308.15 K and 312.15 K. The total potential energy (U_{total}) of the system comprises of the contribution by both bonded and non-bonded interactions. The bonded interaction consists bond stretching (U_b), bond-angle bending (U_a), bond dihedral (U_d) and out of plane distortion (U_{id}) potential. The non-bonded interactions are given by Van der Waals potential or Lennard-Jones Potential (U_{LJ}) and coulomb potential (U_c). Now, the total potential energy is given as[26]

$$U_{total} = U_b + U_a + U_d + U_{id} + U_{LJ} + U_c \tag{4}$$

The harmonic potential represents the bond stretching between two covalently bonded atoms i and j, such that bond stretching potential is given by[26]

$$U_b(r_{ij}) = \frac{1}{2} K_{ij}^b (r_{ij} - b_{ij})^2 \tag{5}$$

where K_{ij}^b is the force constant and b_{ij} is the equilibrium bond length between i and j atoms. The bond-angle vibration between a triplet of atoms $i - j - k$ is represented by a harmonic potential on the angle Θ_{ijk} [26]

$$U_a(\Theta_{ijk}) = \frac{1}{2} K_{ijk}^\Theta (\Theta_{ijk} - \Theta_{ijk}^0)^2 \tag{6}$$

where the force constant is given by K_{ijk}^Θ, angle between atoms is Θ_{ijk} and Θ_{ijk}^o is the equilibrium bond angle.

Proper dihedral angle is defined by dihedral angle (ϕ) between ijk and jkl planes which involves four atoms for formation of the planes. The periodic dihedral potential is given as [26]

$$U_{pd}(\phi_{ijkl}) = k_{ijkl}^c (1 + cos\,(n_{ijkl}\phi_{ijkl} - \phi_o)) \tag{7}$$

where k_{ijkl}^c is the force constant, ϕ_{ijkl} is proper dihedral angle, ϕ_o is the angle where potential passes minimum value and n_{ijkl} is multiplicity. The proper dihedral : Ryckaert-Bellemans potential function is given by [26]

$$U_{RB}(\phi_{ijkl}) = \sum_{n=0}^{5} C_n \left(cos(\psi) \right)^n \tag{8}$$

where $\psi = \phi - \pi^c$; ϕ is dihedral angle and $C_0......C_5$ are Ryckaert- Bellemans parameters.

The nonbonded interatomic interaction is the sum of Lennard-Jones interaction (U_{LJ}) and coulomb interaction (U_c) and given as [26]

$$U(r_{ij}) = U_{LJ}(r_{ij}) + U_c(r_{ij}) \tag{9}$$

$$U(r_{ij}) = 4\epsilon_{ij}\left[\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}}\right)^{6}\right] + \frac{q_i q_j}{4\pi\epsilon_o r_{ij}} \tag{10}$$

where $\sigma_{ij} = \frac{1}{2}(\sigma_{ii} + \sigma_{jj})$, $\epsilon_{ij} = (\epsilon_{ii}\epsilon_{jj})^{\frac{1}{2}}$ and r_{ij} is the cartesian distance between two atoms i and j.
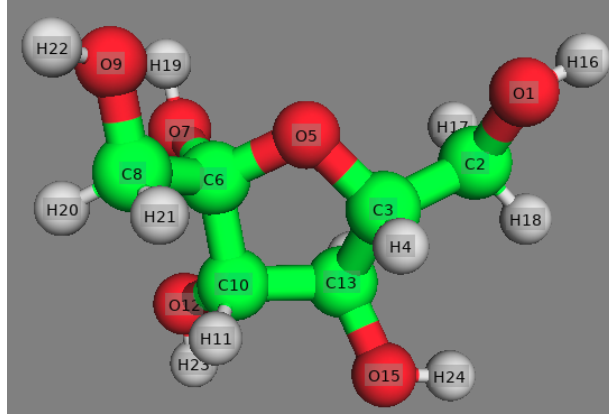
Figure 2. Structure of fructose molecule obtained from *FRU.pdb* file[27].

The bonded parameters for SPC/E water is given in the Table 1.

Table 1. Force-field (bonded) parameters for SPC/E water.

K_{OH} (kJmol^{-1}nm^{-2})	b$_{OH}$ (nm)	K_{HOH} (kJmol^{-1}rad^{-2})	Θ_o
3.4500×10^5	0.1	3.8300×10^2	109.47^o

In Table 1, b_{OH} is the equilibrium bond length between oxygen and hydrogen atoms (O-H) in water molecule. K_{OH} is the force constants of the bonds O-H in water molecule. Similarly, Θ_0 is the equilibrium bond angle (HOH) and K_{HOH} is the strength of the bond angle vibration potential in water molecules.

The non-bonded parameters for oxygen (O9) atom of fructose and water is given in the Table 2.

Table 2. OPLS/AA force-field (non-bonded) parameters for oxygen (O9) atom of fructose and SPC/E water.

O9	Values	Water	Values
σ_{O9-O9}	0.3070 nm	σ_{OW-OW}	0.3165 nm
ϵ_{O9-O9}	85.55 k$_B$	ϵ_{OW-OW}	78.2 k$_B$

The subscripts O9-O9 and OW-OW represent the oxygen-oxygen interaction in fructose molecules and oxygen-oxygen interaction in water molecules respectively. The parameters for SPC/E water presented in the Table 2 are inherent in GROMACS package. The above parameters in Table 2 are for the Lennard-Jones interaction.

The Coulomb interaction in water molecule arises due to the partial charge of hydrogen atom and oxygen atom which have the values +0.4238 e and -0.8476 e respectively [26]. Similarly, the Coulomb interaction for fructose molecule arises due to the partial charge of carbon, hydrogen and oxygen atoms, where e is the elementary (basic unit) charge.
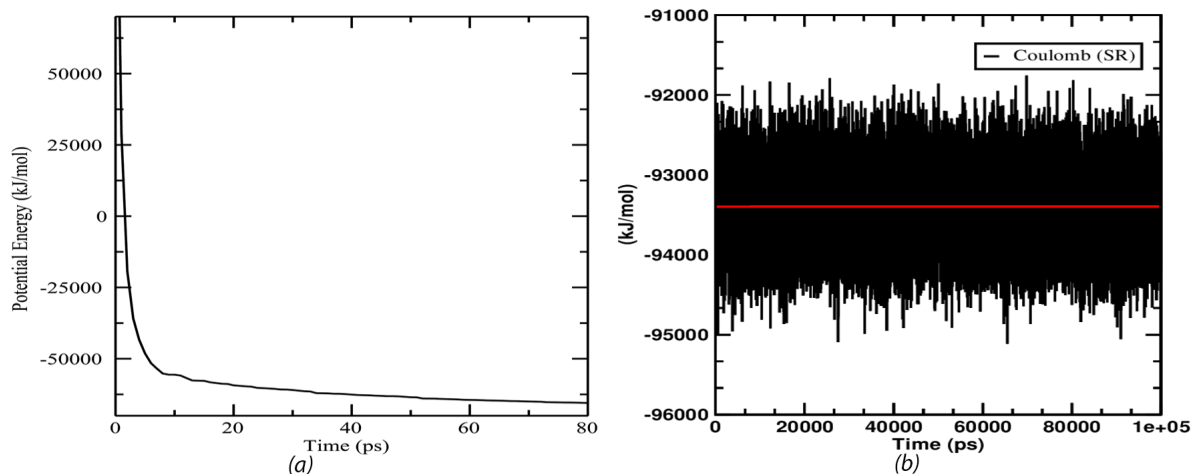
Figure 3. (a) Potential energy as a function of time after energy minimization, (b) Coulomb (short-ranged) potential energy at 298.15 K.

Simulation Procedure

The molecular dynamics (MD) simulation for binary mixture of fructose and SPC/E water was carried out in a cubical box of size 3.7 nm with periodic boundary conditions[14] using GROMACS package and OPLS/AA forcefield. The system was subjected to energy minimization with cut-off restriction of 1 nm to avoid Van der Waals contact caused by the atoms that are too close[18, 22]. The steepest-descent algorithm was used for energy minimization and algorithm stops when the maximum force is less than energy minimization tolerance[26]. The negative potential energy in calculations confirms the energy minimization and local minima of our system. The potential energy of the system after minimization is shown in Fig. 3(a).

The system needs to be in equilibrium state before production run in order to study the dynamical proper-ties. The dynamical variables change with various parameters like temperature, density and pressure. Thus, the system was equilibrated at four different temperatures of 298.15 K, 303.15 K, 308.15 K and 312.15 K and pressure of 1 bar using NPT ensemble to attain the thermal equilibrium. The velocity-rescaling (modified Berendsen) thermostat and Berendsen barostat[26] were used to maintain constant temperature and pressure at coupling time $\tau_t = 0.01$ ps and $\tau_p = 0.8$ ps respectively. The isothermal compressibility of water was taken to be 4.6 $\times$ 10^{-5} bar^{-1}. The system was equilibrated for 100 ns with the time steps of 2 fs (0.002 ns) using leap-frog integrator. The initial velocity was generated according to Maxwell-Boltzmann distribution function at specified temperature[26]. All the bonds are converted to constraint using LINCS algorithm[26]. The Particle Mesh Ewald (PME) algorithm was used for long range interaction. The cut-off parameter of 1 nm was considered with periodic

boundary conditions for coulomb and Lennard-Jones (LJ) interaction[14].

The structure of the system after equilibration is shown in Fig. 4(a). The density and simulated temperatures at different coupling temperatures is shown in Table 3.
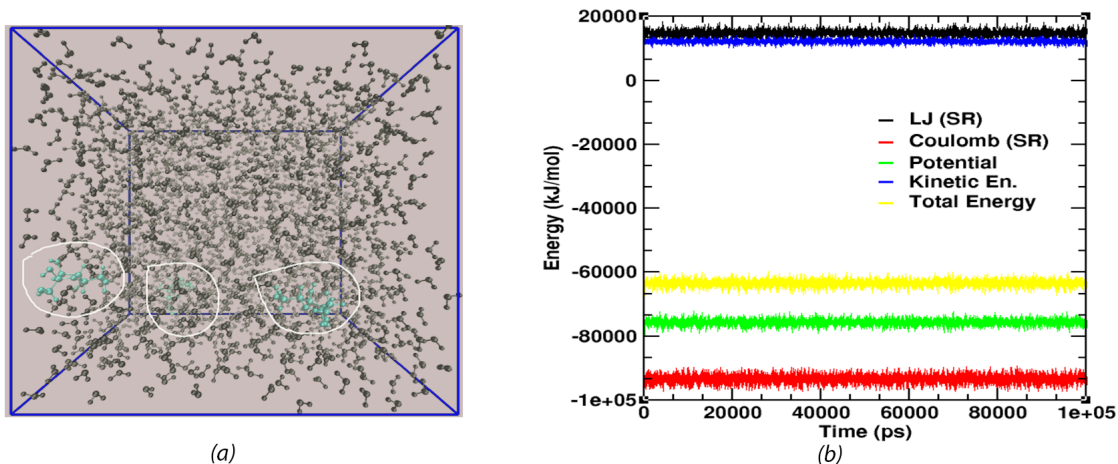
Figure 4. (a) Structure of three fructose molecules (enclosed) and water as solvent after equilibration, (b) Energy profile of the system at T=298.15 K.

Table 3. Values of simulated temperature(T_{sim}) and density at various coupling temperatures(T_{FRU}).

S.N	T_{FRU} (K)	T_{sim} (K)	ρ_{system} (kg/m^3)	ρ_{water} (kg/m^3) [28]
1.	298.15	298.11±0.037	996.12±0.034	997.05
2.	303.15	303.09±0.038	993.44±0.034	995.65
3.	308.15	308.09±0.038	990.73±0.033	994.03
4.	312.15	312.05±0.039	988.39±0.033	992.59

The simulated values of system density are in good agreement (within maximum deviation of around 1%) with that of water density as seen in Table 3. From Table 3, it can be inferred that the density is inversely proportional to the temperature i.e. Higher the temperature, lower is the density. After equilibration run, the production run was performed to calculate the equilibrium properties of the system such as diffusion coefficient by fixing the number of particles, volume and temperature i.e. NVT ensemble. The velocity-rescale thermostat was used for this run. We didn't couple the system to a fixed pressure and had used the structure obtained after equilibration run by which we fixed the volume of the system. The production run was carried out for 100 ns with the time step of 2 fs.

Energy Profile

The Fig. 4(b) represents the energy profile of the system at 298.15 K with the contributions of different energies. In our OPLS/AA force field, the total potential energy is the sum of Lennard-Jones and Coulomb energy. As we have used the cut-off values for Lennard-Jones and Coulomb potential, the energy corresponding to them

are the short range energies. The total energy is the sum of potential and kinetic energies. The Lennard-Jones interaction energy is positive with an average of 14862.76±2.32 kJ mol^{-1}. The Coulomb energy is negative with value of -93395.37±3.78 kJ mol^{-1} so the potential energy, which is the sum of Lennard-Jones and Coulomb energy is negative with value of -75665.15±2.38 kJ mol^{-1}. The Lennard-Jones energy is positive which destabilizes the system, where as the attractive Coulomb interaction keeps the system bound and stable. This shows that the dominating part potential energy is Coulomb energy. The kinetic energy is 12250.45±1.55 kJ mol^{-1}, so the total energy, sum of potential and kinetic energy is -63414.70±2.87 kJ mol^{-1}. The negative value of the total energy shows that the system is bounded and is in stable equilibrium.

3. Results and Discussion

In this section, we present and discuss the structural and dynamical properties with the radial distribution function (RDF), diffusivity of solute (fructose) and solvent itself, respectively, in SPC/E model of water.

Radial Distribution Function

The spherically averaged local organization around any given atom is explained by radial distribution function (RDF) and thus can be used to study structure of the system. RDF, the distribution of the neighboring molecules with respect to the reference molecule, is dimensionless function [22]. In case of periodic systems, RDF shows sharp peaks and troughs up to infinity where the separations and heights are the characteristics of the lattice structure [20]. RDF oscillates up to certain orders and then attains constant value as unity [29]. We evaluate pair distribution function in terms of RDF.

RDF g($\mathbf{r}$) between oxygen atoms of water molecules g$_{(OW-OW)}$($\mathbf{r}$) and oxygen (O9) atom of fructose and oxygen of water molecule i.e. g$_{(O9-OW)}$($\mathbf{r}$) has been evaluated. The value of g($\mathbf{r}$) is zero up to certain region from origin which is called exclusion region. In this region, the probability of finding particle with respect to the reference particle is zero. There is no probability of finding particle below exclusion region if it is lesser than the Van der Waals radius ($2^{\frac{1}{6}}\sigma_{ij}$) or distance of separation is lesser than Van der Waals radius. The exclusion region is due to r^{-12} term of LJ interaction and repulsive coulomb interaction.

The first peak point (FPP) in RDF curve is the point where g($\mathbf{r}$) has the maximum value and corresponding value is first peak value (FPV). The oscillatory behaviour in RDF curve is reduced on going right handside in graph and finally no oscillation is achieved which implies the absence of long range correlation as (g($\mathbf{r}$)→1 [30]). The curve of g($\mathbf{r}$) is oscillatory in nature hence particles are not distributed uniformly around the reference particle rather they are arranged in discrete spherical shell-like structures having certain radius from the central molecule. Therefore, the first peak in g($\mathbf{r}$) signifies position of the first nearest neighbor which is found in first shell and second peak indicates the position of second nearest neighbor in second shell [31].
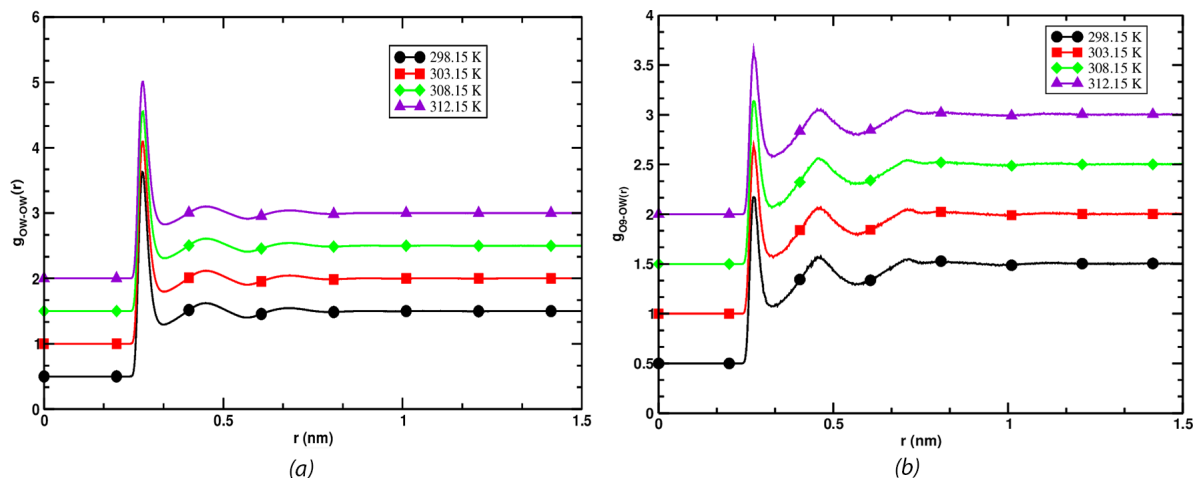
Figure 5. RDF at different temperatures. (a) Oxygen atoms of water molecules, (b) Oxygen atom of fructose molecule and oxygen atom of water molecule.

Fig. 5(a) represents the RDF of oxygen atoms of water molecules at different temperatures. It shows three clear peaks which suggest that the molecules are correlated up to third solvation shell. The value of the peak and position of the peak are provided in Table 4.

Table 4. Simulated data for the RDF analysis between the solvent molecules.

			RDF analysis of OW-OW			
T(K)	ER (nm)	FPP(nm)	FPV	SPP (nm)	SPV	TPP (nm)	TPV
298.15	0.240	0.274	3.128	0.450	1.122	0.680	1.046
303.15	0.240	0.276	3.092	0.450	1.118	0.684	1.044
308.15	0.240	0.276	3.053	0.450	1.110	0.686	1.042
312.15	0.240	0.276	3.010	0.456	1.100	0.690	1.041

Note: ER - Excluded Region, FPP - First Peak Position, FPV - First Peak Value, SPP - Second Peak Position, SPV - Second Peak Value, TPP - Third Peak Position, TPV - Third Peak Value.

The equilibrium structure of the solvent i.e. water molecules is determined by the RDF of solvent. The hydrogen of water does not take part in LJ interaction in SPC/E model that we have used. Hence, $g_{OW-OW}(\mathbf{r})$ is used to study the structure of water molecule. The value of σ for OW-OW is 0.3165 nm, and the Van der Waals radius ($2^{1/6}\sigma$) is 0.3553 nm [26]. From the Table 4, it is clear that the excluded region remains fairly independent of changing temperature. It also calculates that the excluded region is smaller than the Van der Waals radius and nearest neighbor separation indicating that the probability of finding correlated oxygen atoms in this region to be zero. The first peak position remains at the same position within the error of $\pm$ 0.002 nm as a function of temperature. On the contrary, SPP and TPP shift towards right on increasing temperature. The magnitudes of all the peaks decrease on rising temperature. Furthermore, the width of the peaks increases on increasing temperature. Both variations are the consequences of excess volume created in the system and the co-ordination number decreases with increase in temperature. The thermal agitation of atoms in the system

increases with increase in temperature and solvent becomes less structural. The RDF between the oxygen of fructose and oxygen of water describes solute-solvent interaction that broadens the scope of the study is shown Fig. 5(b).

Table 5. Simulated data for the RDF analysis between oxygen (O9) atom of fructose molecule and oxygen atom of water molecule.

T (K)	ER (nm)	FPP (nm)	FPV	SPP (nm)	SPV	TPP (nm)	TPV
			RDF analysis of O9-OW				
298.15	0.238	0.272	1.672	0.464	1.074	0.718	1.049
303.15	0.238	0.272	1.691	0.464	1.068	0.720	1.048
308.15	0.238	0.272	1.638	0.460	1.062	0.710	1.046
312.15	0.238	0.272	1.646	0.464	1.054	0.712	1.046

The detail of the Fig. 5(b) is given in Table (5). The three clear distinct peaks are observed in radial distribution function between the solute and solvent. The magnitude of the excluded region is independent of the change in temperature which is shown in Table 5. The correlation between solute and solvent decreases with increase in temperature which can been seen by decreasing peak value. Further, the oscillatory nature of the curve suggests that the distribution of water molecule around the reference atom isn't uniform. The roughness in the figure is due to insufficient statistics caused by the few number of fructose molecules. The value of σ for O9-OW is 0.31175 nm, and the van der Waals radius ($2^{1/6}\sigma$) is 0.34992 nm. The value is greater than excluded region (0.238 nm) and verifies the theory that there is no correlated atoms in exclusion region.

Diffusion Coefficients
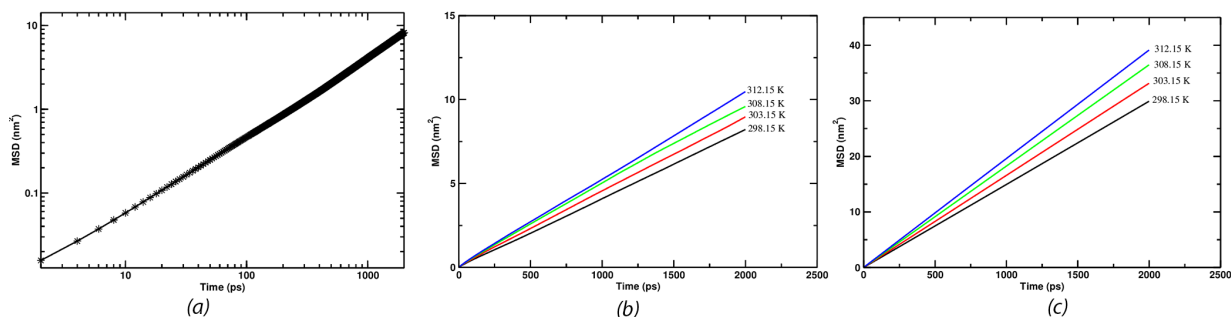
Figure 6. MSD vs time plot. (a) In logarithmic scale for fructose molecule at 298.15 K, (b) Fructose molecule, (c) Water molecule at different temperatures.

In this section we discuss the self-diffusion coefficients of fructose and water molecules which are determined from slope of the mean square displacement (MSD) versus time (t) by using Einstein's relation shown in Eq. 1. The simulation (production run) has been performed for 100,000 ps (100 ns), however, we have taken results upto 2000 ps (2 ns) into our consideration. There is a significant difference between number of fructose and water molecules, hence, results up to 2000 ps has been considered to match our results with the case of infinite dilution.

The high ballistic motion causes diffusion coefficient to be high at first which remains constant as time passes. This constant portion of the graph gives diffusion coefficient [22]. The ballistic region can be seen in Fig. 6(a) which is log-log plot of mean square displacement (MSD) wih time and is represented by the parabolic region of the graph very close to the origin.

The Figs. 6(b) & 6(c) show the MSD plot of fructose and water molecules at temperatures 298.15 K, 303.15 K, 308.15 K & 312.15 K respectively. The data are fitted linearly using *grace* and the slope of MSD curve is divided by 6 to get self-diffusion coefficient. The values of the self -diffusion coefficient of fructose and water obtained from MSD plot is presented in Tables 6-7.

Table 6.   Simulated values of self-diffusion coefficient of fructose at different temperatures.

Self-diffusion coefficient (10^{-9} m^{2}s^{-1})	
T(K)	Simulated value
298.15	0.683 ± 0.00012
303.15	0.746 ± 0.00028
308.15	0.776 ± 0.00076
312.15	0.863 ± 0.00020

From both Table 6 & 7, we can clearly see that self-diffusion coefficient increases with increase in temperature which is infact due to th increase in thermal agitations of molecules. The result of water molecule is compared with the experimental paper and errors are within 8.59%. Thus, the self-diffusion coefficient of water obtained in our simulation is in excellent agreement with the experimental value published in various papers [32**?**].

Table 7.   Simulated and experimental values of self-diffusion coefficient of water at different temperatures.

Self-diffusion coefficient (10^{-9} m^{2}s^{-1})			
T (K)	Simulated value	Experimental value	Error in %
298.15	2.4967 ± 0.000088	2.299 [33]	8.59
303.15	2.7642 ± 0.000046	2.597 [33]	6.43
308.15	3.0417 ± 0.000029	2.895 [33]	5.06
312.15	3.2610 ± 0.000064	3.173 [32]	2.77

The binary or mutual diffusion coefficient is calculated using Darken's relation (Eq. (3)) and is very close to that of self-diffusion coefficient of solute in the mixture due to lower solute concentrations. In our simulation, we have taken 1624 water molecules as solvent and 3 fructose molecules as solute which get dissolved in cubical simulation box. Hence, the mole fraction of water molecules is 0.9982 and that of fructose molecule is 0.0018. These mole fractions along with self-diffusion coefficients are used in Darken's relation to find binary diffusion coefficients presented in Table 8.

Table 8. Simulated and experimental values of binary diffusion coefficient of fructose in water at different temperatures.

	Binary diffusion coefficient (in 10^{-9} m^{2}s^{-1})		
T (K)	Simulated value	Experimental value [34]	Error in %
298.15	0.686 ± 0.00011	0.661 ± 0.008	3.78
303.15	0.749 ± 0.00027	0.744 ± 0.008	0.67
308.15	0.780 ± 0.00069	0.824 ± 0.010	5.35
312.15	0.867 ± 0.00019	0.915 ± 0.010	5.25

The simulated results in this present work are found to be in harmony with the experimental results[34] and errors being within the range of 0.67% to 5.35%.
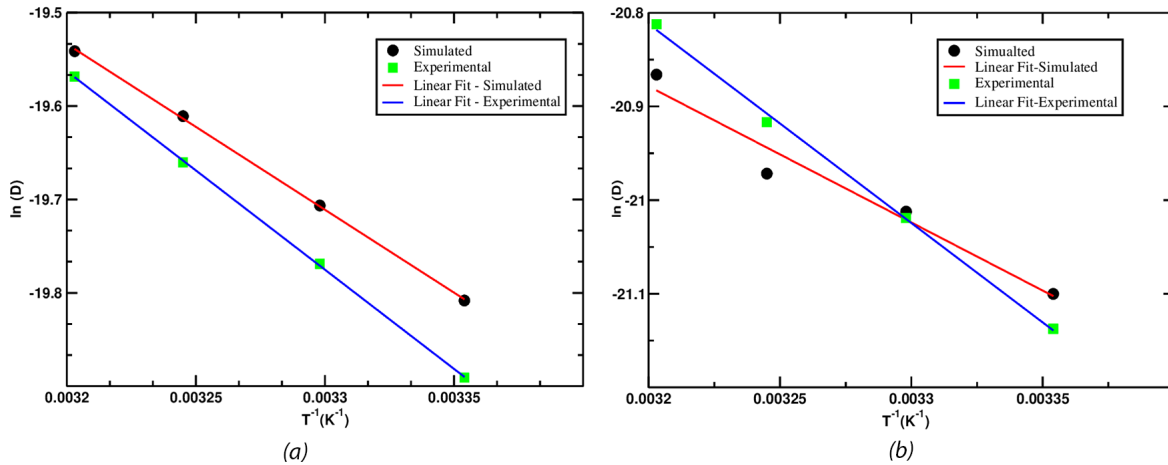
4. Temperature dependence

The diffusion process depends strongly on temperature, being low at low temperature but high at high temperature. This temperature dependency behaviour of the diffusion can be explained by *Arrhenius formula* [35]

$$D = D_o \ \exp\left(\frac{-E_a}{N_A \ k_B \ T}\right). \tag{11}$$

Taking natural logarithm on both sides, we get

$$E_a = -N_A \ k_B \frac{\partial \ln D}{\partial(1/T)}. \tag{12}$$

The intercept of the extrapolate Arrhenius line for $T^{-1} \Rightarrow 0$ yields pre-exponential factor (D_o). Here, the slope of linear best fitted line is used for obtaining activation energy.

Figure 7. Arrhenius diagram of the simulated and experimental values. (a) Water, (b) Binary mixture of fructose and water.

The temperature dependency of diffusion coefficient can be seen in Figs. 7(a) & 7(b). The diffusion coefficient increases with increase in the temperatures. The temperature dependency of diffusion is found to follow Arrhenius behavior when simulated and experimental data are fed in Eq. 11. The Arrhenius diagram is plotted and activation energy is calculated using Eq. 12. Thus, obtained activation energies are presented in Table 9 which are found to be in excellent agreement with experimental value.

Table 9.   Table for calculation of Activation Energy.

Estimation of Activation Energy in $KJmol^{-1}$			
Binary mixture	Activation Energy	Water	Activation Energy
Simulated	12.084	Simulated	15.640 [34]
Experimental	14.748	Experimental	17.657 [32?]

We have plotted the Arrhenius diagram and estimated the activation energy for diffusion shown in Table 9. The experimental value in the Table 9 is the value obtained by using the experimental data of diffusion coefficient for Arrhenius diagram (except for binary mixture which is the value presented in paper) and calculating activation energy from it.

5.   Conclusions

Present work carries the Molecular Dynamics (MD) simulation to study the diffusion coefficient of binary mixture of 3 fructose molecules and 1624 water molecules at different temperatures (298.15 K, 303.15 K, 308.15 K and 312.15 K). The number of molecules of fructose and water were taken in such a way that they mimic the experimental concentration 0.1 mol dm^{-3}. The self diffusion coefficients of water, and the binary diffusion coefficients of the system are found to be in excellent agreement (less than 10%) with the experimental data available in literature. They also follow the *Arrhenius Behavior*. Also, the activation energy of water and the binary mixture (of water and fructose) calculated from the present work agree well with the available experimental values.

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